GCE Examinations Advanced Subsidiary / Advanced Level

Statistics Module S2

Paper D

MARKING GUIDE

This guide is intended to be as helpful as possible to teachers by providing concise solutions and indicating how marks should be awarded. There are obviously alternative methods that would also gain full marks.

Method marks (M) are awarded for knowing and using a method.

Accuracy marks (A) can only be awarded when a correct method has been used.

(B) marks are independent of method marks.



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S2 Paper D - Marking Guide

1. (a)
$$F(5) = 1$$
 M1
 $k(95 - 25 - 34) = 1$; $36k = 1$ $\therefore k = \frac{1}{36}$ A1

(b)
$$P(X > 4) = 1 - F(4)$$
 M1
= $1 - \frac{1}{36} (76 - 16 - 34) = \frac{5}{18}$ A1

(c)
$$f(x) = F'(x) = \frac{1}{36} (19 - 2x)$$
 M1 A1

$$\therefore f(x) = \begin{cases} \frac{1}{36} (19 - 2x), & 2 \le x \le 5, \\ 0, & \text{otherwise.} \end{cases}$$
 A1 (7)

3. (a)
$$H_0: p = \frac{1}{2}$$
 $H_1: p \neq \frac{1}{2}$ B1

(b) let
$$X = \text{no.}$$
 with mobile phones $\therefore X \sim B(25, \frac{1}{2})$ M1
 $P(X \le 7) = 0.0216; \ P(X \le 17) = 0.9784$ M1 A1
 $\therefore \text{ C.R. is } X \le 7 \text{ or } X \ge 18$ A1

(c)
$$0.0216 + 0.0216 = 0.0432$$

(d)
$$H_0: p = \frac{1}{2}$$
 $H_1: p < \frac{1}{2}$ B1
 $P(X \le 8) = 0.0539$ M1
more than 5% : not significant A1 (9)

4. (a) let
$$X = \text{no. of sales per week } :: X \sim \text{Po}(8)$$
 M1
 $P(X \le 4) = 0.0996$ A1

(b) let
$$Y = \text{no. of sales per day } \therefore Y \sim \text{Po}(\frac{4}{3})$$
 M1

$$P(Y > 2) = 1 - P(Y \le 2)$$
 M1

$$= 1 - e^{-\frac{4}{3}}(1 + \frac{4}{3} + \frac{(\frac{4}{3})^2}{2})$$
 M1 A1

$$= 1 - 0.8494 = 0.1506 \text{ (4sf)}$$
 A1

(c)
$$P(X \le 12) = 0.9362$$
; $P(X \le 13) = 0.9658$ M1 A1
 \therefore need 13 in stock A1 (10)

- (a) $13 \times \frac{1}{90} = \frac{13}{90}$ or 0.1444 (4sf) 5. M1 A1
 - (b) $P(44.5^{\circ} \text{ to } 45.5^{\circ}) :: \frac{1}{90}$ M1 A1
 - (c) $P(< 10^{\circ}) = 10 \times \frac{1}{90} = \frac{1}{9}$ **A**1

let $X = \text{no. of times} < 10^{\circ}$ $\therefore X \sim B(10, \frac{1}{9})$ M1

$$P(X > 2) = 1 - P(X \le 2)$$

$$= 1 - \left[\left(\frac{8}{9} \right)^{10} + 10 \left(\frac{1}{9} \right) \left(\frac{8}{9} \right)^9 + \frac{10 \times 9}{2} \left(\frac{1}{9} \right)^2 \left(\frac{8}{9} \right)^8 \right]$$
M1 A1

= 1 - 0.9094 = 0.0906 (3sf) A1 (10)

- 6. let X = no. absent per lesson $\therefore X \sim \text{Po}(2.5)$ $P(X \ge 6) = 1 - P(X \le 5) = 1 - 0.9580 = 0.0420$ M1 A1
 - (b) assumes absences occur independently and at constant rate ill students may infect others and rate may vary at different times **B**3 of year but assumptions fairly reasonable
 - (c) registers for all classes **B**1
 - (d) let $Y = \text{no. absent per } 30 \text{ lessons } \therefore Y \sim \text{Po}(75)$ M1use N approx. $A \sim N(75, 75)$ M1 $P(Y \ge 96) \approx P(A > 95.5)$ M1

 $= P(Z > \frac{95.5 - 75}{\sqrt{75}}) = P(Z > 2.367)$ **A**1

= 1 - 0.9909 = 0.0091**A**1

less than 5% : significant, there is evidence of more absent per lesson **A**1 (12)

(a) $\int_{0}^{3} k(t-3)^{2} dt = 1$ 7. M1

> $k \int_{0}^{3} t^{2} - 6t + 9 dt = 1$ M1

> $\therefore k[\frac{1}{3}t^3 - 3t^2 + 9t]_0^3 = 1$ A1

 $\therefore k[(9-27+27)-(0)]=1; 9k=1; k=\frac{1}{9}$ M1 A1

(b)

 $E(T) = \int_0^3 t \times \frac{1}{9} (t - 3)^2 dt = \frac{1}{9} \int_0^3 t^3 - 6t^2 + 9t dt$ M1 $= \frac{1}{9} \left[\frac{1}{4} t^4 - 2t^3 + \frac{9}{2} t^2 \right]_0^3$ **A**1 $= \frac{1}{9} \left[\left(\frac{81}{4} - 54 + \frac{81}{2} \right) - (0) \right] = \frac{3}{4}$ M1 A1

 \therefore mean time = $\frac{3}{4} \times 10 = 7.5 \text{ s}$ A1

(d) $E(S) = \int_0^2 s \times \frac{1}{12} (8 - s^3) ds = \frac{1}{12} \int_0^2 8s - s^4 ds$ M1 $=\frac{1}{12}\left[4s^2+\frac{1}{5}s^5\right]_0^2$ **A**1 $=\frac{1}{12}[(16-\frac{32}{5})-(0)]=\frac{4}{5}$

 \therefore new mean = $\frac{4}{5} \times 10 = 8 \text{ s}$ \therefore increased by 0.5 s A₁ (18)

> Total (75)

M1 A1

B3

Performance Record – S2 Paper D

1	2	3	4	5	6	7	Total
c.d.f., p.d.f.	modelling	binomial, hyp. test	Poisson	rect. dist., binomial	Poisson, hyp. test., sampling, N approx.	p.d.f., mean	
7	9	9	10	10	12	18	75
	p.d.f.	p.d.f.	p.d.f. hyp. test	p.d.f. hyp. test	p.d.f. hyp. test binomial	p.d.f. hyp. test binomial hyp. test., sampling, N approx.	p.d.f. hyp. test binomial hyp. test., sampling, N approx.